**Written Assignment 1**

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**Question1.**

There are two cases of recursion. One is A[mid] > x and another is A[mid]<x, the basis case is left right or A[mid]=middle. Both the recursions of the two cases are the T(n/2).

1

4

1

1

1

2+T(n/2)

2+T(n/2)

1

. In the times recursion, let , . So, the computational cost of this algorithm is .

**Question2.**

， in the times recursion.

Let the , . So, the upper bound of the algorithm is



, in the times recursion.

Let the ,

The upper bound is .

, in the times recursion.

Let the ,

The upper bound is .

, in the times recursion.

Let the

The upper bound is .

Question3.

(1). In the case 1:

The total time cost:

In the case 2:

Both the two cases are

(2) There are three layers of nested loops,

The first loops out: (Times of getting into loop is n)

Times of getting into second loop: because

)

The second loops out:

Times of getting into second loop: (Sum of geometric sequence)

The second loops out:

To conclude, the total time cost is: (.

So

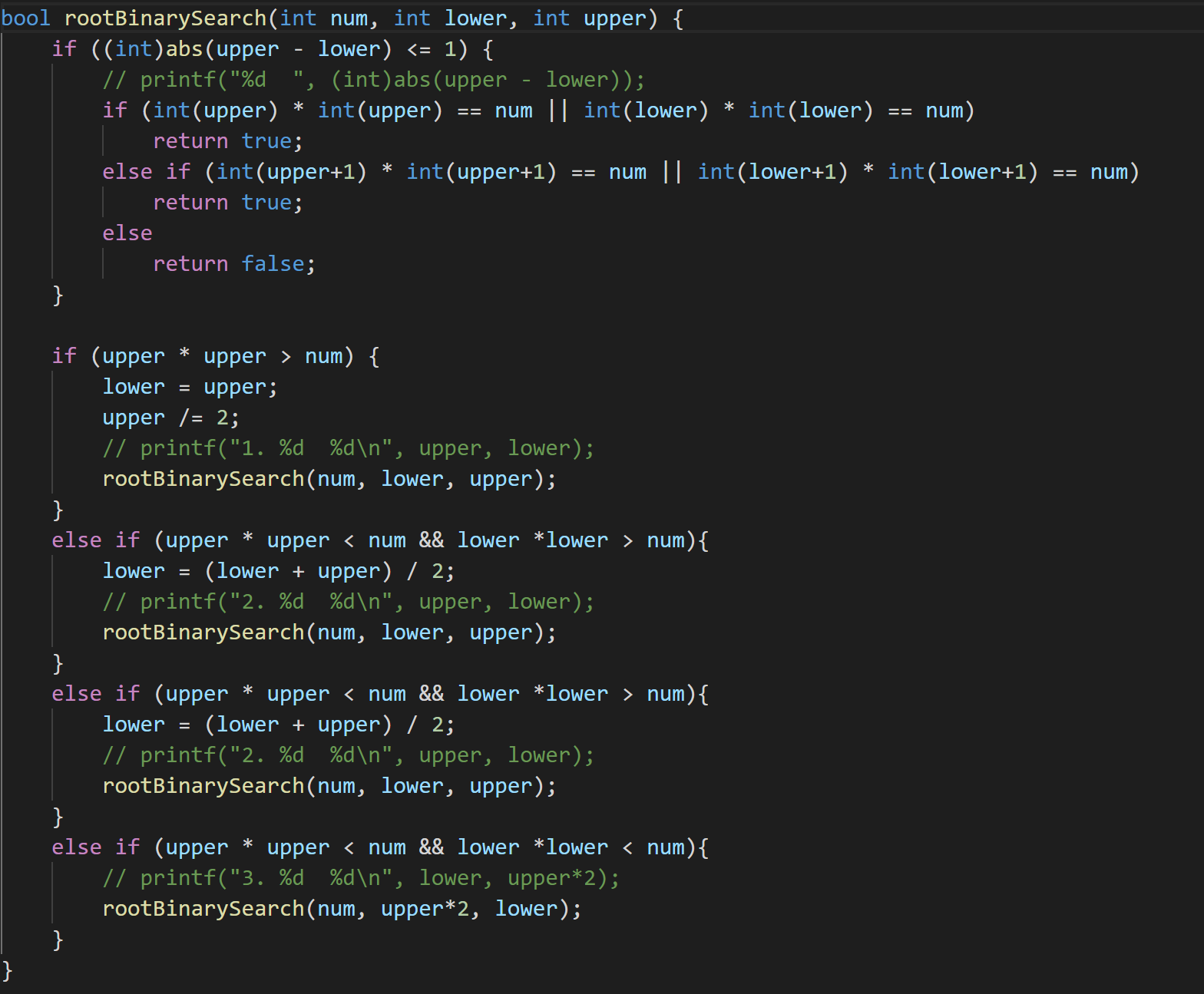
(3)

in the times iteration.

When ,

So, time cost is: .

Question4.



)

)

E

The first case of iteration:

The second case of iteration:

Let , ,

For any number into this function, it should cost log(n) time whether it get into the first case or the second case. To conclude, the time cost of this algorithm is .

Question5.

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        RETURN ( - 1) + ( -2) + ( -3);

We know that:

If there is one steps, the way is: {}

If there are two steps: the way is: {**1,1**}, {**2**}

If there are three steps: the way is {**1,1,1**}, {**1,2**}, {**2,1**},{**3**}

If there are four steps: the way is: {1, **1,1,1**}, {1, **1,2**}, {1, **2,1**}, {1, **3**}; {2, **1,1**}, {2, **2**}; {3, **1**}

We can find that:

Except for the first element, the case is same as the total of others. That is because the first element can be seen as the first steps you get. Therefore, the left is the case you can find.

Since the iterations must be more the others. It should take more time cost because if let it iteration, there will be: . By that analogy to the basis case,

,

, in the times iteration.

Let . So, the time cost is:

Question6.

Divide all the items into [] sets in which each, except possibly the last, contains 4 items. It just pays the . For each set, we should sort the 4 items and find the median one. The time cost is the () . Take these medians and put them in another array. In the recursively calculate the median of these medians. So, the time cost of the recursion is . In other part, we should calculate the partition the original array by the pivot. If the p is the pivot of the array, p is the beginner of array and the r is the ender. ()

We can find the how many elements are greater or less than x at least. There are sets which exists a median is bigger than pivot at least. Except the set contains x and the set with fewer than 4 items. There are only sets with more than 2 items greater than the pivot. So, there are at least items greater than pivot. In the contrary, there are at most items smaller than pivot. .

Induction:

must be greater than . For all the c and a is positive and c is large enough.

So the induction is false and we cannot say that the algorithm run in the linear time.